



Zdychia, 17th–21st September 2024

ON THE DYNAMICS OF A MATHEMATICAL MODEL OF VIRUS SPREADING INCORPORATING THE EFFECT OF A VACCINE BY GÖKÇE ET AL. (NONLINEAR ANALYSIS: REAL WORLD APPLICATIONS 2024)

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ABSTRACT

We study a model of virus spreading incorporating the effect of a vaccine proposed in [1] by Gökçe *et al.* This model is based on a system of six differential equations describing the flow between five compartments in epidemic model with the influence of the vaccine. This influence is described by Hill function with coefficients n and κ .

In the original article [1] the authors focused on calculating \mathcal{R}_0 , the coefficient being a threshold for local stability of a disease free equilibrium (DFE), which strongly depends on the coefficient n , as well as a backward bifurcation for $n = 2$.

In our analysis we used standard Routh-Hurwitz Criterion to prove the local stability of the DFE state for $\mathcal{R}_0 < 1$, and the global stability of this state under some more restrictive condition, based on Kamgang and Sallet approach [2]. We also attempted to estimate the number of positive steady states and study their stability for arbitrary n .

REFERENCES

- [1] A. Gökçe, B. Gürbüz, and A.D. Rendall: *Dynamics of a mathematical model of virus spreading incorporating the effect of a vaccine*, *Nonlinear Analysis: Real World Applications* **78** (2024), 104097.
- [2] J.C. Kamgang and G. Sallet: *Computation of threshold conditions for epidemiological models and global stability of the disease-free equilibrium (dfe)*, *Mathematical Biosciences* **213** (2008), 1–12.