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ON A KINETIC TYPE MODEL OF AUTOIMMUNE DISEASE

Mikhail Kolev[1], Iveta Nikolova[2]

[1]Faculty of Mathematics and Computer Science, University of Warmia and Mazury
ul. Sloneczna 54, 10-710 Olsztyn,
[2]Faculty of Mathematics and Natural Sciences, South-West University "N. Rilski",
ul. I. Mihajlov 66, 2700 Blagoevgrad, Bulgaria
[1] kolev@matman.uwm.edu.pl, [2] iveta.nikolova@abv.bg

ABSTRACT

We consider a mathematical model of autoimmune disease. The model is described by a bilinear system of three integro-differential equations of Boltzmann type. We present numerical results illustrating several typical outcomes of autoimmune disease.

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